



Original Article

# Improved Particle Swarm Optimization of Three-Dimensional Path Planning for Fixed Wing Unmanned Aerial Vehicle

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**Abstract:** Path planning for Unmanned Aerial Vehicle (UAV) targets at generating an optimal global path to the target, avoiding collisions and optimizing the given cost function under constraints. In this paper, the path planning problem for UAV in pre-known 3D environment is presented. Particle Swarm Optimization (PSO) was proved the efficiency for various problems. PSO has high convergence speed yet with its major drawback of premature convergence when solving large-scale optimization problems. In this paper, the improved PSO with adaptive mutation to overcome its drawback in order to applied PSO the UAV path planning in real 3D environment which composed of mountains and constraints. The effectiveness of the proposed PSO algorithm is compared to Genetic Algorithm, standard PSO and other improved PSO using 3D map of Daklak, Dakrong and Langco Beach. The results have shown the potential for applying proposed algorithm in optimizing the 3D UAV path planning.

**Keywords:** UAV, Path planning, PSO, Optimization.

## 1. Introduction

An Unmanned Aerial Vehicle (UAV) is designed for the applications such as inspection, monitoring, and dangerous missions. Today, there is the large interest worldwide in the

development of UAV for the number of smart agricultures, environment monitoring, border patrol, disaster assistance and many others. Whenever a mission is defined, path planning is the crucial element of whole system. In general, path planning targets at generating an optimal global path to the target, avoiding collisions with obstacles, and optimizing the given cost function under constraints.

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Simple 2D path planning algorithm is not able to deal with complex 3D environment, where there are quite a lot of structures constraints and uncertainties. Therefore, in the 3D environment the 3D path planning algorithm for UAV navigation are urgently need nowadays, especially in complex environments such as forest, cave, and urban areas as shown in Figure 1.

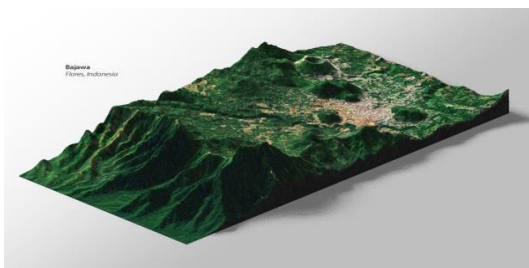


Figure 1. Example of 3D environment.

Scholars have done a great deal of success in path planning to solve such problems such as: 3D Voronoi [1], Probabilistic Roadmap Method [2]. There are some useful optimal search algorithms such as A\* [3] or D\* [4]. These researches are only focus on some methods that are broadly used and not conducive to solve complicated problem because of great computation time and data size [5]. On applying bio-inspired planning algorithms, as in [6] Genetic Algorithm was applied, in [7, 8] Particle Swarm Optimization was improved, Differential Evolution was also proposed in [9], etc. These are algorithms with high efficiency in finding the optimal solution of the problems.

PSO is well known for its lower computational costs, simple principle, higher efficiency and widely used to solve path planning problems [10]. However, PSO has the drawback of a premature convergence when solving complicated optimization problems [11]. Therefore, this research puts forward an improved PSO algorithm by adding adaptive mutation step to optimize the trajectory of UAV.

The rest of this paper is organized as follows. Section 2 provides the techniques to represent the environment and trajectory of

UAV and the cost function. Section 3 provides bio-inspired algorithm PSO and improved one. Experimental results and discussions are presented in Section 4 to evaluate the effectiveness of optimization algorithms. Finally, we conclude the paper in Section 5.

## 2. Environment and cost function modeling

For pre-known 3D path planning, the world space is discretized to represent the 3D environment. The environment, trajectory, obstacle will be defined as following.

### 2.1. Environment and trajectory modeling

In this work, the planning problem was determined in three-dimensional space. The representations of the workspace and trajectory are generally the first step of path planning process for UAV. To apply optimization algorithms to the trajectory planning problem, the environment is encoded into a representation which is suited for UAV's path and algorithms. In this phase, the 2D grid is created where each element of the matrix specifies the elevation of terrain [12]. Environment and path representations are shown in Figure 2.

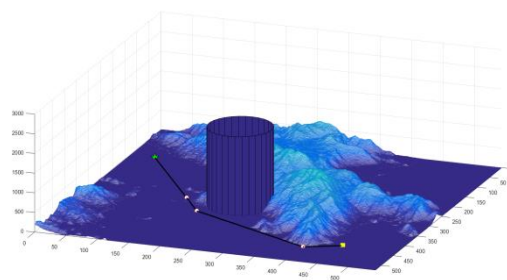


Figure 2. 3D visualization of environment and trajectory.

In Figure 2, the circle markers represent the way-points of the UAV path, the black line connecting the way-points represents the trajectory of an UAV and the blue cylinders represent the cylindrical danger zones to be avoided.

The final trajectory is created by connecting all the way-points. A matrix is used where each row represents the coordinates of  $i$ -th way-points, as shown in (1).

$$\text{trajectory} = \begin{bmatrix} x_1 & y_1 & z_1 \\ x_2 & y_2 & z_2 \\ \dots & \dots & \dots \\ x_n & y_n & z_n \end{bmatrix} \quad (1)$$

## 2.2. Cost function and constraints modeling

The danger zones are kept in sub-matrices where each row represents the coordinates  $(x_i, y_i)$  and  $d_i$  is the diameter of the  $i$ -th cylinder. The danger zone is defined as follows:

$$\text{danger zones} = \begin{bmatrix} x_1 & y_1 & d_1 \\ x_2 & y_2 & d_2 \\ \dots & \dots & \dots \\ x_n & y_n & d_n \end{bmatrix} \quad (2)$$

The path planning problem is formulated as an optimization of the following cost function including path length, flight altitude, collision and danger zones avoidance. With assumption of having enough fuel, the cost function in [12] is simplify as:

$$F_{\text{cost}} = F_{\text{length}} + F_{\text{altitude}} + F_{\text{collision}} + F_{\text{danger zones}} \quad (3)$$

where  $F_{\text{length}}$  and  $F_{\text{altitude}}$  denote the terms of path length and UAV fly height to evaluate a candidate route, respectively.  $F_{\text{collision}}$  penalizes paths colliding with the ground and  $F_{\text{danger zones}}$  is the penalty term while paths going through danger zones.

It is believed that the length of an optimal route should be as short as possible. Then  $F_{\text{length}}$  can be written as follows:

$$F_{\text{length}} = 1 - \left( \frac{L_{P_1 P_2}}{L_{\text{traj}}} \right) \quad (4)$$

therefore

$$F_{\text{length}} \in [0,1] \quad (5)$$

where  $L_{P_1 P_2}$  is distance of the straight line from the starting point to the destination point and  $L_{\text{traj}}$  is the total length of the actual trajectory.

It is obviously that the UAV should fly as low altitude as possible, but the decrease of the altitude will increase the crash probability with

the ground and mountain. The flight altitude cost function of the path is defined as follows:

$$F_{\text{altitude}} = \frac{A_{\text{traj}} - Z_{\text{min}}}{Z_{\text{max}} - Z_{\text{min}}} \quad (6)$$

therefore

$$F_{\text{altitude}} \in [0,1] \quad (7)$$

where  $Z_{\text{max}}$  is the upper bound of the height in our search space,  $Z_{\text{min}}$  is the lower bound and  $A_{\text{traj}}$  is the average altitude of the actual trajectory.  $Z_{\text{max}}$  and  $Z_{\text{min}}$  are respectively set to be slightly above the highest and lowest points of the terrain.

As flying into the danger zones with the missile and radar, the UAV may encounter the risk of being discovered and attacked from the enemies. The term used to penalize the violation of UAV to the danger zones is defined as follows:

$$F_{\text{danger zones}} = \frac{L_{\text{inside d.z}}}{\sum_{i=1}^n d_i} \quad (8)$$

with

$$F_{\text{danger zones}} \in [0,1] \quad (9)$$

where  $n$  is the total number of danger zones,  $L_{\text{inside d.z}}$  is the path length into the threat sources zones for a route and  $d_i$  is the diameter of the  $i$ -th danger zone. Since it is possible for  $L_{\text{inside d.z}}$  to be larger  $\sum_{i=1}^n d_i$  (as in the case of a dog-leg path through a single danger zone),  $F_{\text{danger zones}}$  is set to 1.

In order to avoid the collision with the mountain and ground in the environment, the flight altitude should be higher than the elevation of the terrain. This function is depicted as:

$$F_{\text{collision}} = \begin{cases} 0, & L_{\text{under terrain}} = 0 \\ P + \left( \frac{L_{\text{under terrain}}}{L_{\text{traj}}} \right), & L_{\text{under terrain}} > 0 \end{cases} \quad (10)$$

with

$$F_{\text{collision}} \in 0 \cup [P, P + 1] \quad (11)$$

where  $L_{\text{under terrain}}$  is the total length of the trajectory which travels below the ground level and  $L_{\text{traj}}$  is the total length of the trajectory. For this function, additional penalty term  $P$  is set to be 3. Therefore, when the value of the evaluation function  $F$  is greater than 3.5, the planning path can be considered as a non-feasible one. The altitude of the terrain and the

altitude of the trajectory are compared in a discrete way using the Bresenham's line drawing algorithm [13].

After determining the cost function, optimization algorithms will be used to find the optimal path by minimizing the cost value. The optimal trajectory satisfies four criteria that are represented by the cost function.

### 3. Improved particle swarm optimization

PSO is a population based stochastic optimization technique that finds optimal root by updating generations [14]. PSO simulates the food searching behavior of fish herd or bird flock. In the PSO, each particle of swarm always searches in its searching space to replace old position with the new best position. The searching process using PSO includes four steps (except step four) and improved PSO includes five steps as described below:

1. *Initialize*: Generate the population and evaluate the objective (fitness) function.

2. *Update personal best and global best*: Check each particle for new personal best. If the current position is better than personal best, it becomes personal best. Otherwise, the personal best remains the same. If any particle in the swarm holds a personal best that is better than global best, it becomes leader and its personal best becomes global best.

3. *Update velocity and position of all particles*: The position and velocity are updated using the following equations:

$$v_i(t) = wv_i(t - 1) + a_1u_d(p_i(t - 1) - x_i(t - 1)) + a_2U_d(g(t - 1) - x_i(t - 1)) \quad (12)$$

$$x_i(t) = x_i(t - 1) + v_i(t)\Delta t \quad (13)$$

in which  $v_i$  is the velocity of the  $i$ -th particle;  $x_i$  is its position in search space;  $p_i$  is the personal best of  $i$ -th particle;  $g$  is the global best of the swarm;  $u_d$  and  $U_d$  are random values in the range of [0,1];  $w$ ,  $a_1$ ,  $a_2$  are respectively inertia, personal influence and social influence parameters.

4. *Adaptive mutation*: The position of particle  $x_i$  will be mutated by using Gaussian mutation as:

$$x^*_i(t) = x_i(t) * (1 + m * gaussian(\sigma)) \quad (14)$$

in which  $x^*_i(t)$  is a particle after the mutation,  $\sigma$  is set to 10% of search space,  $m = 1/t$  is the adaption coefficient which decreasing by the number of iterations. Compared with adaptive mutation in [15, 16], the effect of mutation is controlled by  $m$  for fine turning when particle reach global optimal and overcome the local optimal.

5. *Terminate searching process or continue searching*: The process is terminated if *i*) The current step is equal to latest step or *ii*) The swarm has converged (radius of the swarm is smaller than  $10^{-3}\%$  of search space size). Otherwise, come back to step 2.

The flowchart of standard PSO and Improved PSO with adaptive mutation is shown in Figure 3.

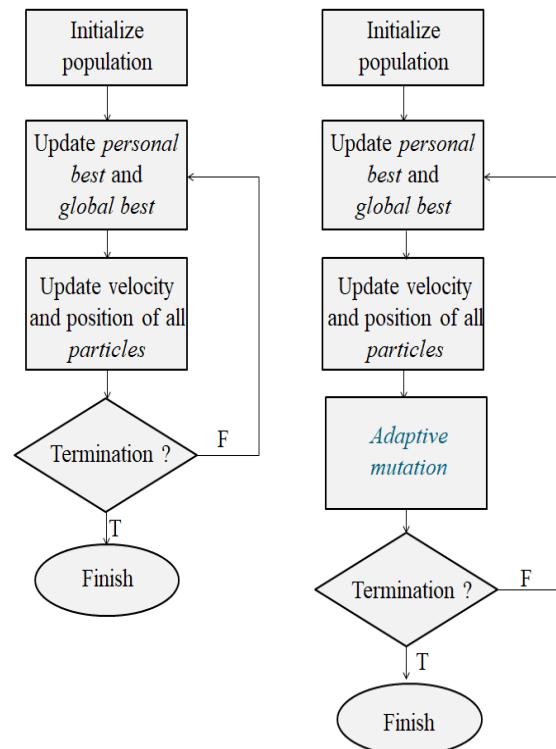


Figure 3. The proposed PSO algorithm.

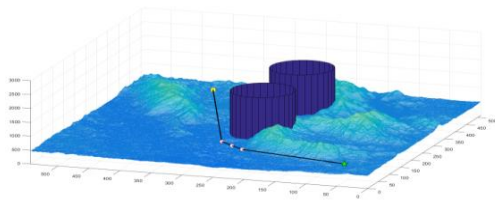
### 4. Experimental results

In this section, simulation results are presented using the proposed approach. We compare the performance of the four algorithms using different scenarios of three real terrain elevation maps from Vietnam (Daklak, Dakrong and Langco Beach). The digital elevation maps for the three real terrains were taken from The Global Data Explorer repository [17] to satisfy real environment requirements. All environments have been chosen in order to search for path lines between mountains, plains and sea. In addition, some danger zones are randomly distributed to increase the complexity of environment. 3D visualizations of the computed paths of three terrains are shown in Figure 4 and parameters of them are shown in Table 1.

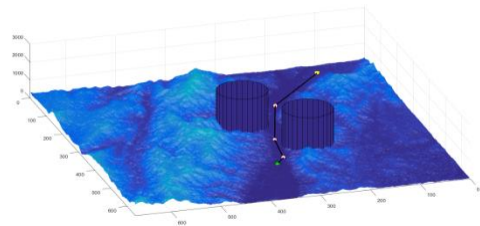
Table 1. Parameters of Daklak, Dakrong and Langco maps

Map	Area (km)	Min-Max altitude (km)
Daklak	16.32×15.4	9.33-33.42
Dakrong	19.59×20.1	0.09-28.08
Langco	15.72×16.02	0-38.1

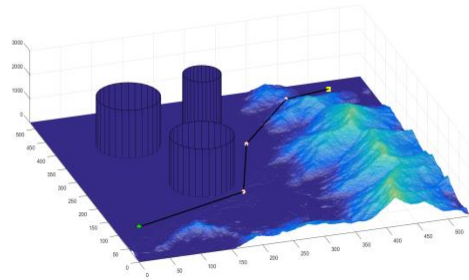
In order to illustrate the superiority of the improved algorithm, the comparison simulation was conducted between the proposed Improved PSO algorithm with adaptive mutation and Improved PSO in [8]. In this reference, authors added a method to dynamically adjust the inertia weight factor  $\omega$  and the personal influence  $a_1$  and social influence  $a_2$  parameters according to the change of the search process. Figure 5 show the cost value comparison curve of the two algorithms.



a) Daklak

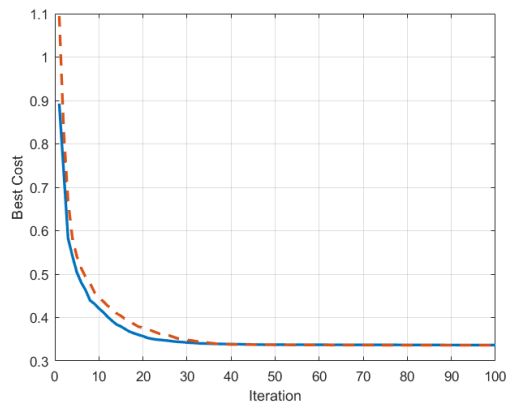


b) Dakrong

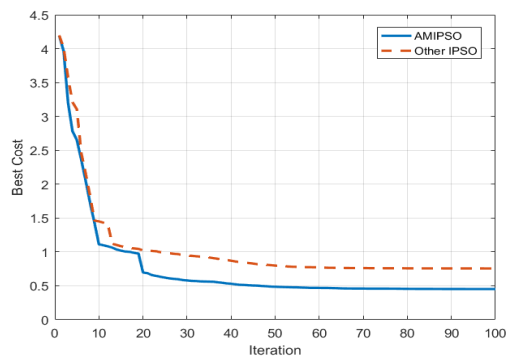


c) LangCo

Figure 4. Optimal path planning of three maps.



a) Daklak



b) Dakrong

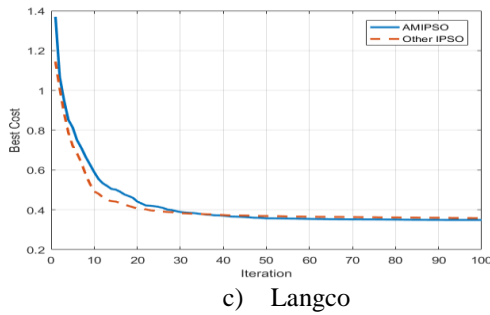


Figure 5. Comparison of cost function for 3 maps.

All of four algorithms (GA, PSO, proposed Improved PSO and Improved PSO) have been tested under three different scenarios. In each terrain, each algorithm is run 10 times and we calculate the cost function average and standard deviation. A solution is considered better than others if its cost function is smaller. A stable algorithm should have lower cost function standard deviation. The cost values obtained by running four optimization algorithms are shown in Table 2.

Table 2. Results

Terrain	Cost value ± standard deviation			
	GA	PSO	PSO in [8]	Improved PSO
Daklak	0.3381± 0.0007	0.3562± 0.0012	<b>0.3363±</b> <b>0.0001</b>	0.3366± 0.0001
Dakrong	1.5707± 3.4002	1.3245± 2.2532	0.7547± 1.1049	<b>0.4527±</b> <b>1.0193</b>
LangCo	0.3856± 0.0015	0.3964± 0.0021	0.3548± 0.0002	<b>0.3546±</b> <b>0.0002</b>

In Table 2, it is shown that standard PSO algorithm does not perform better than GA in most cases, but the improved PSO with adaptive mutation algorithm shows significantly more efficiency, demonstrating the reliability of the algorithm for applying to practical problems.

Traditional PSO, GA or Improved PSO in [8] can be easily trapped in local optimums because of many local optimal traps in complex

search space like Langco. Therefore, it is more difficult to find the global optimal solution. In comparison to other improved PSO algorithm in [8], Improved PSO with adaptive mutation is not too superior and efficiency is quite similar in Daklak and Langco maps. However, for applying in difficult scenario of Langco, Improved PSO with adaptive mutation was able to perform much better than other algorithms and this result shows the effectiveness of the proposed algorithm. Adaptive mutation can maintain the population diversity throughout the algorithm run by changing position of particles using Gaussian mutation. Proposed algorithm is superior to PSO, GA and Improved PSO [8] in jumping out local optimums as well as improving the algorithm convergence ability effectively.

### 5. Conclusion

In this research, offline UAV path planning problem which need considering a real 3D environment and known obstacles is tackled. Meta-heuristic approaches (GA, standard PSO and improved PSO) were used to optimize the trajectory. It is practically proved that improved PSO produces better path and especially has dominant stability compared to the others. With such a high stability of improved PSO, we expect it will also perform well in more complex path planning problem. In future research, the smooth constraint will be considered for smooth trajectory.

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